I[[Z_iYkii_edi"ijWji"WdZWkj^ehfhe\<u>b</u>[i\ehj^ifkXb<u>YWje</u>dWJO^jjfi**%**mmm\$[i[Wh/^]

Chadhef 15 High-Qi alihmEaflmMath: Leafning and Teaching With Tfajechofieg and Technologieg

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ABSTRACT



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High-quality Early Math:

AB AC !

! "#%& '()*+, -#\$+, .\$-(&', .:3+/%*1;\$)#6#+) - "9<+6#.\$)# :#=#/('&#, *\$2)(&&<%)*"\$"; &+*"#&+*%-+//1;\$"#\$-)%*%-+ &+*">\$? #\$.#6-)%<#\$"#\$.#=; !#+-"%, 4\$8%" ``\$A#+), %, 4\$!) -"%'. "((.\$#.3-+*()6;\$')(2#) :"%'.)#, \$2)(&&<%)*"\$*(\$F"#\$4) :#=#/('&#, *\$*")(34"%, 9'#) *#+-"%, 4\$+, .\$/#+), %, 4>SG%, ./#+), %, 4\$!)

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BAC : C A A A C

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 $\begin{array}{l} 3@, 3^{*"}, \&7\#^{*} < , 3@^{*8} - \% \$7^{"} / /^{*}.(*, *(3\&\% - /^{*}; \&'' \cdot .23\%\&^{*}\%K^{*7}, 3''\&^{*}, 2@.'': '<^{-3^{*}0} ! \&, 1'' \$ (8.4^{*}PQQ \backslash T^{*}], 3.\% - , 7^{*} \\ & , 3@^{"} < , 3.2(^{*}D': ..(\%\&\#^{*} =, -''74^{*}PQQ \backslash 4^{*}(62@^{*7}'', \&^{-.-/^{*}\%}; ; %\&36 - .3\#^{*}/, ; (*, \&^{''}; ''\&^{-.2}.\%6(^{*}0 > 7, "(('' - (*''3^{*}, 764^{*}PQQ \backslash T^{*}], 3.\% - , 7^{*} \land .3@^{"} < , 3.2(^{*}D': ..(\%\&\#^{*} =, -''74^{*}PQQ \backslash T^{*}], 3.\% - , 7^{*} \land .3@^{"} < , 3.2(^{*}D': ..(\%\&\#^{*} =, -''74^{*}PQQ \backslash T^{*}) \\ \end{array}$

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O@"*&"(", &2@*, - '*'"(./ -*%K*3@"*+", &-.-/*, - '*O", 2@.-/*\$.3@*+", &-.-/*O&, 1"23%&."(4*1+Om!,*3%%74* 7,6-2@"'*.-*PQPQ*K%77%\$.-/*P*#", &(*%K*'":"7%; <"-34*

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 $\begin{array}{c} O@^{**30} \& ^{*} \& ^{*} ; & \& ^{3*} \& & \& ^{*} & ^{7''} , \& - . - /^{*3} \& , 1 ^{*} 23 \& \& \#^{*} 2\% - (. (3(^{*} \& \mathbb{K}^{*} 3'' , 2@ . - /^{*} \& , 23.2 ^{''} (d'' - : . \&) - <'' - 3(4^{*} . - 3'' \& , 21.) & (d\mathbb{K} - ^{''} \mathbb{I} 36 - ^{''} \mathbb{K} \& \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \& \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \& \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \& \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \& \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \& \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \& \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \& \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \& \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \& \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \otimes \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \otimes \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \otimes \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \otimes \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \otimes \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \otimes \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \otimes \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \otimes \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 7^{*} \mathbb{K} \otimes \mathbb{K}^{*} 2@ ? 1 ^{''} \mathbb{I} 8 ^{''} 2@ ? 1 ^{''} \mathbb{I} 8 ^{''} 2@ ? 1 ^$

 $\begin{array}{c} D((\%2.,3.\%-*K\%\&^*i\%6-/*>@.7'\&''-*0]\,DB\,i>Y^*,-'*3@''^*]\,,3.\%-,7^*>\%6-2.7^*\%K^*0'',2@''\&(*\%K^*\wedge,3@''<,3.2(*0]\,>0\,^{\circ}YG^*0@\&\%6/@^*3@.(*K''''F,284^*('':''\&,7^*\&''))) \\ \end{array}$

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 $D(*; \&":.\%6(7#*'.(26(("'4*, -*. < ; \%\&3, -3*2\% < ; \% - "-3*\%K*@./@IC6, 7.3#* < , 3@*.(*3", 2@. - /*; \&, 23.2"(*3@, 3*@) - %&**2@.7'&"-Z(*26736\&"(4*K, < 7."(4*. - '.:.'6, 7*2@, \&, 23"\&.(3.2(4*, (*$"77*, (*3@".&*; , 33"\& - (*K*3@. - 8. - /*, - '*"), & -. - /*0) - & ; "-3"&*"3*, 764*PQRXT*A&#"*"3*, 764*PQRAY6*O@.(*2, -*F"*; , & 3.267, & 7#*2@, 77" - /. - /*. - *3@"*2% - 3"J3*%K*"3"2@ - %7% / #4*, (*3@"("*; "& (% - , 7*2@, & , 23"&.(3.2(*, & "* < %(3*(" - (.3.:"7#*&"(; % - ''' *3%*. - *3@"*2% - 3"J3*%K*; "& (% - , 7*&), & 3@**2% - 3"J3*%K*"3"2@ - %7% / #4*, (*3@"("*; "& (% - , 7*2@, & , 23"&.(3.2(*, & "* < %(3*(" - (.3.:"7#*&"(; % - ''' *3%*. - *3@"*2% - 3"J3*%K*; "& (% - , 7*&), & 3.% - (@.:; (6*E - *3@.(*("23.% - 4* $"*''' (2& F"*; & % < .(. - /*&"(", & 2@*, - '*'': "7%; < "-3*"KK%&3(*3%*, ': %2, 3"*K%&*; ; & (% - , 7*&), & & (*3@"("*2@, 77" - / (*3%*; & %): .''' < , 3@*"J; "& .'' - 2"(*K%&*3%', ', #Z(*/7%F, 7*2.3.N" - (4*(.36, 3"'*. -*(%2, .7*&), & 3*%K*; ; & (% - , 7*&), & & (*3*, 3*@"*'', 5&, 7.(3.2*(%2."3#6*M''*2% - 3*%K*; .76. - /*, - '*F%7(3"&. - /*, *<%&"*; 76&, 7.(3.2*(%2."3#6*M''*2% - "23*3@.(*3%*-" $*K", 36&"(*% - *[LT]^2.$

 $\begin{array}{c} 0@''*g - .3'' *W3, 3''(*@, (*F''' - *''J; "\&." - 2. - /*, *'\%6F7''*; , - ''' < .2*d*, *: .\&6(*, 33, 28. - /*\&''(; .\&, 3\%\&\#*(\#(3'' < (*, - '*, */\&\% \$. - /*, \$, \&'' - ''((*\%K*7\% - /I(3, - '. - /*. - ''C6.3."(*. -*'' '62, 3.\% - ,7*\&''(\%6\&2''(4*''J, 2''\&F, 3'' '*F\#*) > L hE9 IRS4*K\%\&*57, 284*E - '. / '' - \%6(4*, - '*; ''\%; 7''*\%K*2\%7\%\&*05E=L > Y*, - '*2@.7'&'' - *\$.3@*'.(, F.7.3."((* ^ %(3*')))) > 0.5*(*.5)$

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